



Write the transformations. Be sure to include the amplitude, period & phase shift.

$$y = \frac{5}{4} \tan\left(\frac{\pi}{4}x - 2\right) + 3$$

parent:  $y = \tan x$  amp = -  
 $\rho = \pi$   
 $\rho.s. = -$

1)  $y = \frac{5}{4} \tan x$  v.s. by  $\frac{5}{4}$

2)  $y = \frac{5}{4} \tan\left(\frac{\pi}{4}x\right)$  h.s. by  $\frac{\pi}{4}$   $\rho = 4$

3)  $y = \frac{5}{4} \tan\left(\frac{\pi}{4}\left(x - \frac{8}{\pi}\right)\right)$  shift right  $\frac{8}{\pi}$   $\rho.s. = \frac{8}{\pi}$

4)  $y = \frac{5}{4} \tan\left(\frac{\pi}{4}x - 2\right) + 3$  shift up 3

Practice - Write the transformations:

$$y = -2 \sec(-5x + \pi) + 3$$

parent:  $y = \sec x$  amp = -  
 $\rho = 2\pi$   
 $\rho.s. = -$

1)  $y = -\sec x$   $r_x$

2)  $y = -\sec(-x)$   $r_y$

3)  $y = -2\sec(-x)$  v.s. by 2

4)  $y = -2\sec(-5x)$  h.c. by  $\frac{1}{5}$   $\rho = \frac{2\pi}{5}$

5)  $y = -2\sec\left(-5\left(x - \frac{\pi}{5}\right)\right)$  shift right  $\frac{\pi}{5}$   $\rho.s. = \frac{\pi}{5}$

6)  $y = -2\sec(-5x + \pi) + 3$  shift up 3

Write the transformations.

$$f(x) = \frac{1}{3} \cot\left(-\frac{3}{4}x + \frac{\pi}{4}\right) + 2$$

parent:  $f(x) = \cot x$  amp = -  
 $P = \pi$   
 $P.S. = -$

1)  $f(x) = \cot(-x)$  r y

2)  $f(x) = \frac{1}{3} \cot(-x)$  v.c. by  $\frac{1}{3}$

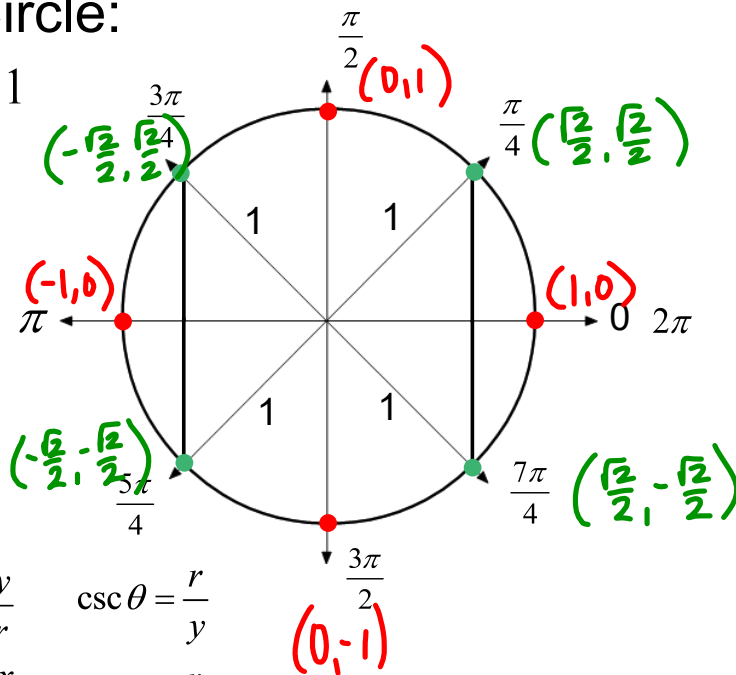
3)  $f(x) = \frac{1}{3} \cot\left(-\frac{3}{4}x\right)$  h.s. by  $\frac{4}{3}$   $P = \frac{4\pi}{3}$

4)  $f(x) = \frac{1}{3} \cot\left(-\frac{3}{4}\left(x - \frac{\pi}{3}\right)\right)$  shift right  $\frac{\pi}{3}$   $P.S. = \frac{\pi}{3}$

5)  $f(x) = \frac{1}{3} \cot\left(-\frac{3}{4}x + \frac{\pi}{4}\right) + 2$  shift up 2

Unit Circle:

$r = 1$

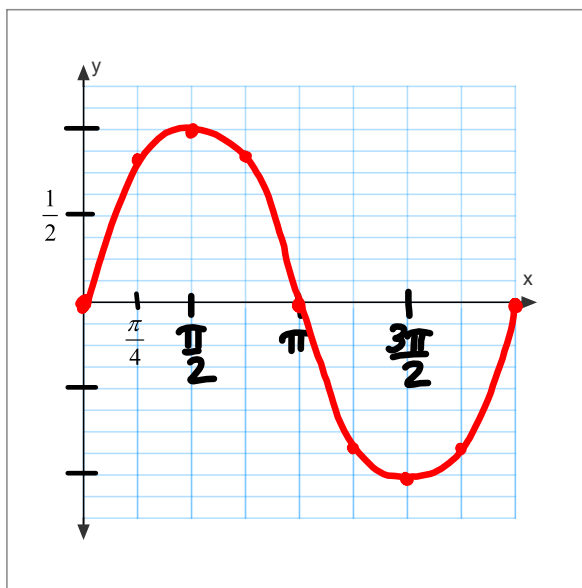


$$\begin{aligned} \sin \theta &= \frac{y}{r} & \csc \theta &= \frac{r}{y} \\ \cos \theta &= \frac{x}{r} & \sec \theta &= \frac{r}{x} \\ \tan \theta &= \frac{y}{x} & \cot \theta &= \frac{x}{y} \end{aligned}$$

Parent Functions:

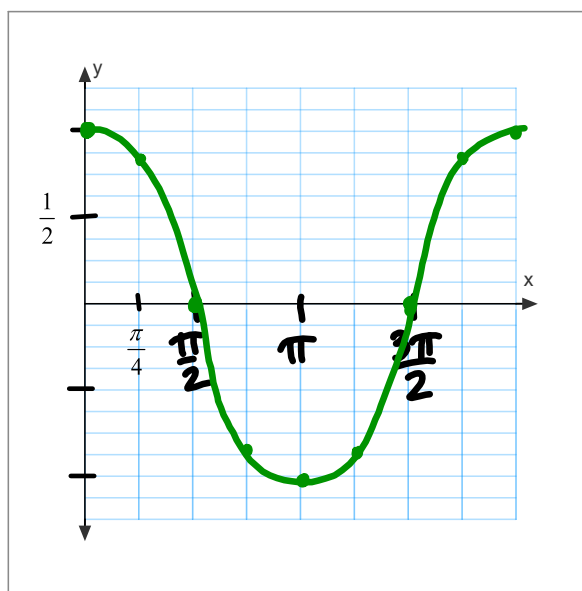
$y = \sin x$

$x$	$y$
0	0
$\frac{\pi}{4}$	$\frac{\sqrt{2}}{2} \approx .707$
$\frac{\pi}{2}$	1
$\frac{3\pi}{4}$	$\frac{\sqrt{2}}{2}$
$\pi$	0
$\frac{5\pi}{4}$	$-\frac{\sqrt{2}}{2}$
$\frac{3\pi}{2}$	-1
$\frac{7\pi}{4}$	$-\frac{\sqrt{2}}{2}$
$2\pi$	0



$y = \cos x$

$x$	$y$
0	1
$\frac{\pi}{4}$	$\frac{\sqrt{2}}{2}$
$\frac{\pi}{2}$	0
$\frac{3\pi}{4}$	$-\frac{\sqrt{2}}{2}$
$\pi$	-1
$\frac{5\pi}{4}$	$-\frac{\sqrt{2}}{2}$
$\frac{3\pi}{2}$	0
$\frac{7\pi}{4}$	$\frac{\sqrt{2}}{2}$
$2\pi$	1



## Assignment:

Graph the remaining parent functions.